

SPAF: Sub-texel Precision Anisotropic Filtering

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Agenda

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- ❑ Introduction
- ❑ Background and Previous Works
- ❑ Goals
- ❑ SPAF
 - ❖Algorithm
 - ❖H/W Cost Minimization
 - ❖Image Quality and H/W Cost Comparison
- ❑ Conclusions & Future Works

Introduction

□ Limitations with Tri-linear Filtering

- ❖ Blurring

➔ Severe artifacts
in the rendered image



➔ Due to approximation
of footprint to square
(Shape of footprint: Quadrilateral)

➔ Box Filter

Background

□ Anisotropic Filtering - reference to David B. Kirk (1998)

- ❖ Adjust filtering to the **shape** of footprint, as well as **size**

- ❖ **High Quality** vs.
More Texels and Computations

- ❖ Considerations

➔ **LOD Selection**: Load More texels necessary for filtering

➔ **Shape**: Approximate the footprint shape Better

➔ **Filter**: Need Good filter

Previous Works (1)

- Two Approaches in Algorithm & H/W Architecture
 - ❖ Assemble tri-linear filter probes
 - ➔ TEXRAM(Footprint Assembly)
 - ➔ Feline(Fast Elliptical Lines)
 - ❖ Apply an area coverage weight to the texel
 - ➔ Fast Footprint Mip-mapping

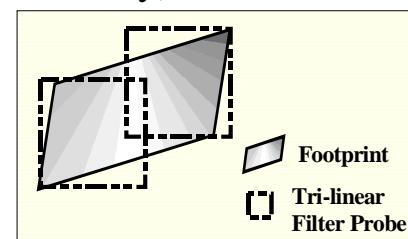
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Previous Works (2)

- TEXRAM(Footprint Assembly)
 - ❖ Increase in Tri-linear Filter Probes
 - ➔ Require Many Texels
 - ❖ Box Filter
- Feline(Fast Elliptical Lines)
 - ❖ Accurate Calculation of Filter Probe Number
 - ➔ 2 x Number of Filter Probes in TEXRAM
 - ❖ Gaussian Filter



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Previous Works (3)

Previous Works

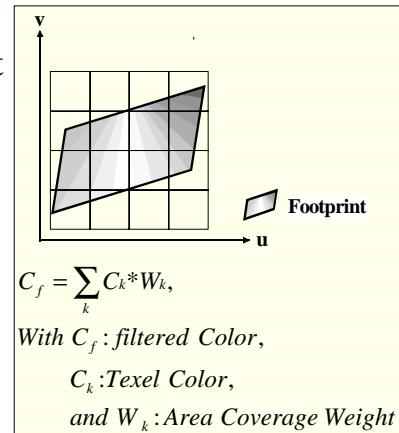
□ Fast Footprint Mip-mapping

- ❖ LOD Selection using Aspect ratio of footprint

- ❖ Area Coverage Weight

- ➡ with Significant Quantization Error
- ➡ Large Weight Table

- ❖ Box Filter



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Goals

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□ To Provide

- ❖ SPAF Algorithm

- ➡ Filtering algorithm under limited number of texels(M)
- ➡ with LOD Selection Using Aspect Ratio of Footprint
- ➡ with Sub-texel Precision Area Coverage Weight
- ➡ using Gaussian Filter

- ❖ H/W Cost Minimization

- ➡ Sub-texel Precision Area Coverage Weight Table Minimization

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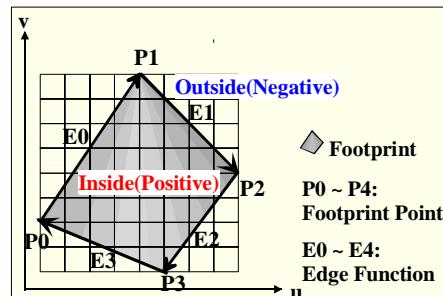
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Characteristics of Edge Function

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- Footprint is represented by Four Edge Functions
- Edge Function
 - based on Andreas Schilling (1991)
 - ❖ Sign of Edge Function
 - ➔ Inside or Outside
 - ❖ Absolute value of Edge Function
 - ➔ Manhattan distance between an edge and a point



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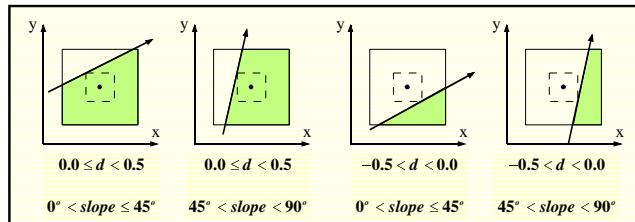
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Area Coverage of Texel

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- ❖ $A = f(\text{slope}, d)$, with A : Area Coverage,
 slope: Slope of Edge,
 and d : Value of Edge function

- ➔ $d < -0.5$: No area coverage
- ➔ $d > +0.5$: Full area coverage
- ➔ $-0.5 < d < +0.5$: Partial area coverage
 : slope determines the shape and size of partial area coverage



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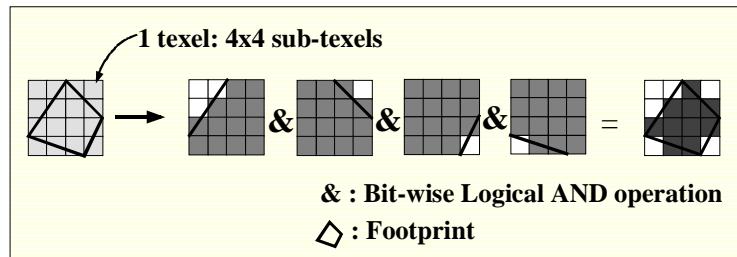
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Sub-texel Precision Area Coverage Generation

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- Intersection of four sub-texel masks of the footprint



- ❖ Sub-texel mask table size: 4KBytes
 $\Rightarrow 2^5(\text{edge slope}) \times 2^6(\text{edge function}) \times 2^4\text{bits}(4 \times 4 \text{ sub-texel mask})$
- ❖ Sub-texel mask table size **per texel**: 16KBytes

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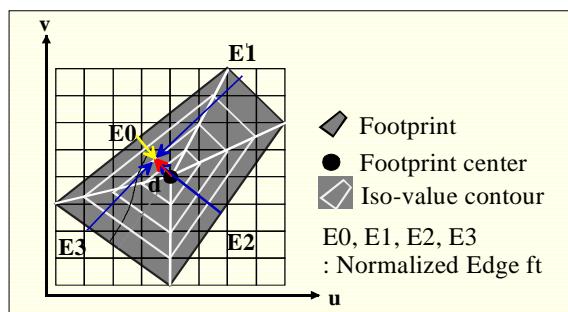
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Gaussian Filter

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- $W_G = \exp(-a*d^2)$,
With a : filter coefficients,
 d : Normalized distance from the center to the texel
- Relation Equation: $\underline{I} = \underline{d} + \underline{E}$
 - ❖ $\underline{E} = \min\{E0, E1, E2, E3\}$



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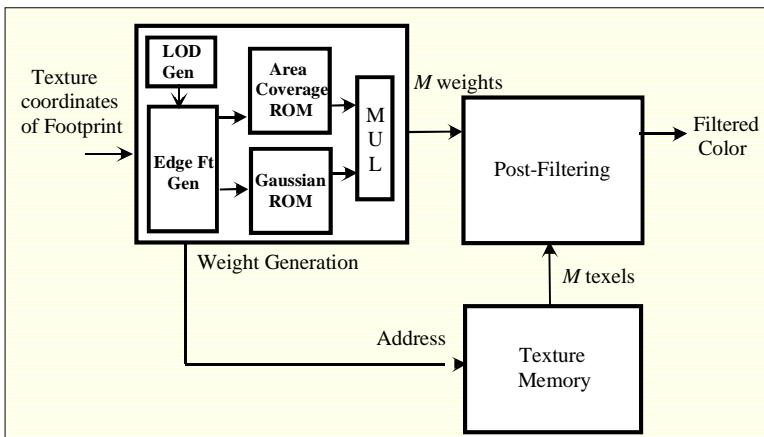
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H/W Architecture

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- Area Coverage ROM size
: 16KBytes x M , for M texels



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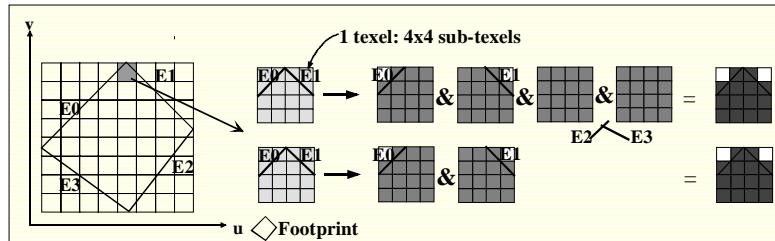
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Observations On Sub-Texel Mask

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❖ Observations I

- ⇒ Fully Covered Sub-texel Mask has No Effect on Partial Area Coverage Generation



❖ Observations II

- ⇒ The number of texels which **four or three** edges cross is FEW
- ⇒ In Most texels, edges **Less than three** cross

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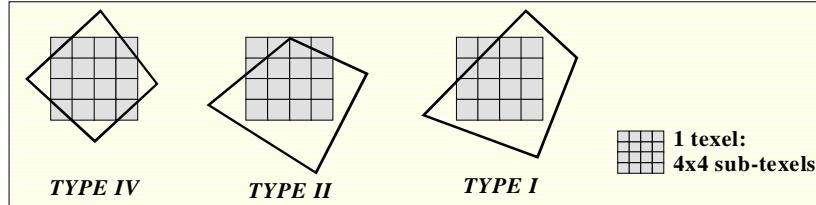
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Texel Type Classification

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□ Texel Type Definition

- ❖ *Type IV*: Texel which four or three edges cross
 - ⇒ Four sub-texel mask ROMs (16KBytes)
- ❖ *Type II*: Texel which two edges cross
 - ⇒ Two sub-texel mask ROMs (8KBytes)
- ❖ *Type I*: Texel which one edge crosses or no edges cross
 - ⇒ One area coverage ROM (1KBytes)



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Number of Texel Type

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❖ Simulation Results used to Obtain Number of Texel Type

| | | Max. Num. of Occurrence | Three Simulation Cases |
|----------|----------|-------------------------|---|
| $M : 16$ | Case I | 6 | Case I : Occurrence of Only Type IV |
| | Case II | 12 | |
| | Case III | 16 | |
| $M : 32$ | Case I | 6 | Case II : Occurrence of Both Type IV and Type II (i.e. Type IV + Type II) |
| | Case II | 24 | |
| | Case III | 32 | |
| $M : 64$ | Case I | 6 | Case III : Occurrence of All Types |
| | Case II | 32 | |
| | Case III | 64 | |

❖ Number of each Texel Type is given as

- ➔ Type IV : Case I
- ➔ Type II : Case II – { Type IV i.e. Case I }
- ➔ Type I : Case III – { (Type IV + Type II) i.e. Case II }
- ➔ Ex) At $M = 16$, Type IV = 6, Type II = 6, and Type I = 4

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Quality of Image

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❖ SNR(Signal to Noise Ratio)

→ T_{image} : test image, R_{image} : reference image

$$10 \log_{10} \frac{\sum_{i,j} T_{image}(i,j)^2}{\sum_{i,j} |T_{image}(i,j) - R_{image}(i,j)|^2} \text{ (dB)}$$

❖ Simulation Condition

→ Texture: Checkerboard and text with 256x256 resolution

→ Image resolution: 640x480

→ Reference image: Elliptical Weighted Average(EWA)

→ Test image: Feline,
TEXRAM,
FFM(Fast Footprint Mip-mapping),
and SPAF(Sub-texel Precision Anisotropic Filtering)

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Image Quality Comparison

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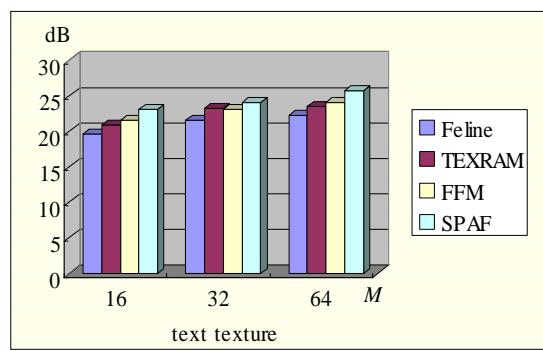
❖ Simulation Results & Comparison

→ Feline achieves **Lowest SNR**

→ At $M = 32$ or 64 , TEXRAM **rivals** FFM

→ At $M = 16$, FFM achieves **Higher SNR** than TEXRAM

→ SPAF achieves **Highest SNR**



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Test Scene

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- ❖ Test scenes with text font texture at $M = 16$



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H/W Cost Comparison

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- ❖ Area coverage table size at $M = 16 \sim 64$

ROM Size Based On Texel Type

| | TYPE IV (16KB) | TYPE II (8KB) | TYPE I (1KB) | Total Size |
|----------|----------------|---------------|--------------|------------|
| $M : 16$ | 6 | 6 | 4 | 148KBytes |
| $M : 32$ | 6 | 18 | 8 | 248KBytes |
| $M : 64$ | 6 | 26 | 32 | 336KBytes |

ROM Size Comparison of Two Algorithms

| | Fast footprint mip-mapping | SPAF (Non- Minimization) | Ratio | SPAF (Minimization) | Ratio |
|----------|-------------------------------|-----------------------------|--------|------------------------|--------|
| $M : 16$ | 286K x 2 = 572KBytes | 16K x 16 = 256KBytes | 2 : 1 | 148KBytes | 4 : 1 |
| $M : 32$ | 3.5M x 2 = 7MBytes | 16K x 32 = 512KBytes | 14 : 1 | 248KBytes | 28 : 1 |
| $M : 64$ | 6.6M x 2 = 13.2MBytes | 16K x 64 = 1024KBytes | 13 : 1 | 336KBytes | 40 : 1 |

► 1/2(4) ~ 1/13(40) of fast footprint mip-mapping

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Conclusions & Future works

Conclusions

□ Proposed Key Schemes

- ❖ Filtering algorithm using the sub-texel precision area coverage and Gaussian filter weight
- ❖ Area coverage ROM minimization based on texel types

□ Proposed Algorithm & Architecture achieves

- ❖ Quality of image **Superior to** other algorithms at the **Same** loaded number of texels
- ❖ H/W cost **Smaller** than fast footprint mip-mapping So, **Amenable** to H/W implementation

□ Future Works

- ❖ Texture Cache & Effective filtering at the Magnification

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